Lazily Aggregated Quantized Gradient Innovation for Communication-Efficient Federated Learning

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Abstract—This paper focuses on communication-efficient federated learning problem, and develops a novel distributed quantized gradient approach, which is characterized by adaptive communications of the quantized gradients. Specifically, the federated learning builds upon the server-worker infrastructure, where the workers calculate local gradients and upload them to the server; then the server obtain the global gradient by aggregating all the local gradients and utilizes it to update the model parameter. The key idea to save communications from the worker to the server is to quantize gradients as well as skip less informative quantized gradient communications by reusing previous gradients. Quantizing and skipping result in ‘lazy’ worker-server communications, which justifies the term Lazily Aggregated Quantized (LAQ) gradient. Theoretically, the LAQ algorithm achieves the same linear convergence as the gradient descent in the strongly convex case, while effecting major savings in the communication in terms of transmitted bits and communication rounds. Empirically, extensive experiments using realistic data corroborate a significant communication reduction compared with state-of-the-art gradient- and stochastic gradient-based algorithms.

Index Terms—federated learning, communication-efficient, gradient innovation, quantization

1 INTRODUCTION

TRAINING today’s machine learning functions (models) relies on an enormous amount of data collected by a massive number of mobile devices. This comes with substantial computational cost, and raises serious privacy concerns when the training is centralized. In addition to cloud computing, these considerations drive the vision that future machine learning tasks must be performed to the extent possible in a distributed fashion at the network edge, namely devices [2].

When distributed learning is carried out in a server-worker setup with possibly heterogeneous devices and datasets as well as privacy considerations, it is referred to as federated learning [3]. The server updates the learning parameters utilizing the information (usually gradients) collected from local workers, and then broadcasts the parameters to workers. In this setup, the server obtains the aggregate information without requesting the raw data—what also respects privacy and mitigates the computation burden on the server. Such a learning paradigm however, incurs communication overhead that does not scale with the number of workers. This is aggravated in deep learning, which involves high-dimensional learning parameters. In fact, communication delay has become a bottleneck for fully exploiting the distributed computing resources to speed up the training of machine learning models [5,6].

In this context, communication-efficient federated learning methods have gained popularity recently [3]. Most methods build on simple gradient updates, and are centered around gradient compression to save communication, including gradient quantization and sparsification, as outlined in the following overview of the prior art in this area.

1.1 Prior art

Quantization. Today’s computers usually utilize 32 or 64 bits to quantize the floating point number, which is assumed to be accurate enough in most algorithms. By quantization in this paper, we mean fewer bits are employed. Toward the goal of reducing communications, quantization compresses transmitted information (e.g., the gradient) by limiting the number of bits that represent floating point numbers, and has been successfully applied to several engineering tasks employing wireless sensor networks [7]. In the context of distributed machine learning, a 1-bit binary quantization scheme has been proposed in [8,9]. Multi-bit quantization methods have been developed in [10,11], where an adjustable quantization level endows flexibility to balance the communication cost and the convergence rate. Other variants of quantized gradient schemes include ternary quantization [12], variance-reduced quantization [13], error compensation [14], and gradient difference quantization [11,15]; and it is shown in [11] that the linear convergence rate can be maintained with gradient difference quantization.

Sparsification. Sparsification amounts to discarding some entries of the gradient and the most straightforward scheme is to transmit only gradient components with large enough magnitudes [16]. Surprisingly, the desired accuracy can be attained even with 99% of the gradients being dropped in some cases [17]. To reduce information losses, gradient components with small values are accumulated and then applied
We first review the standard distributed server-worker learning architecture that typically aims at solving an optimization problem of the form

\[
\min_{\theta} \sum_{m \in M} f_m(\theta) \quad \text{with} \quad f_m(\theta) := \sum_{n=1}^{N_m} \ell(x_{m,n}; \theta) \tag{1}
\]

where \( \theta \in \mathbb{R}^d \) denotes the parameter to be learned; \( M \) with \( |M| = M \) is the set of workers; \( x_{m,n} \) represents the \( n \)-th data vector at worker \( m \) (e.g., feature vector and its label); \( N_m \) is the number of data samples at worker \( m \); while \( \ell(x; \theta) \) denotes the loss associated with \( \theta \) and \( x \); and \( f_m(\theta) \) stands for the local loss corresponding to \( \theta \) and all data at worker \( m \). For ease in exposition, we further let \( f(\theta) := \sum_{m \in M} f_m(\theta) \) denote the overall loss function.

Throughout this paper, we consider implementing distributed gradient descent (GD) in the commonly employed worker-server setup. Since the data samples are distributed across the workers, in each iteration the workers need to download the model parameter from the server, calculate the local gradient using local data and upload the gradients to the server; upon receiving all the local gradients, the server then updates the parameter vector following the GD iteration

\[
\theta^{k+1} = \theta^k - \alpha \sum_{m \in M} \nabla f_m(\theta^k) \tag{2}
\]

where superscript \( k \) indexes the iteration, \( \alpha \) is the stepsize, and \( \nabla f(\theta^k) := \sum_{m \in M} \nabla f_m(\theta^k) \) is the aggregated (or, global) gradient. It is clear that to implement (2), the server has to communicate with all workers to obtain ‘fresh’ gradients \( \{\nabla f_m(\theta^k)\}_{m=1}^{|M|} \). In several settings though, communication is much slower than computation \[3\]. Thus, as the number of workers grows, worker-server communications become the bottleneck \[33\]. This becomes more challenging when adopting popular deep learning models with high-dimensional parameters, and correspondingly large gradients. This clearly prompts the need for communication-efficient learning.

Before introducing our communication-efficient learning approach, we revisit the canonical form of popular quantized (Q) GD methods \[8\]-\[15\] in the simple setup of (1) with one server and \( M \) workers:

\[
\text{QGD:} \quad \theta^{k+1} = \theta^k - \alpha \sum_{m \in M} Q_{m}(\theta^k) \tag{3}
\]

where \( Q_{m}(\theta^k) \) is the quantized gradient that coarsely approximates the local gradient \( \nabla f_m(\theta^k) \). While the exact quantization scheme varies across algorithms, transmitting \( Q_{m}(\theta^k) \) generally requires fewer bits than transmitting its accurate counterpart \( \nabla f_m(\theta^k) \). Similar to GD however, only when all the local quantized gradients \( \{Q_{m}(\theta^k)\} \) are collected, the server can update \( \theta \).

In this context, the present paper puts forth a quantized gradient innovation method (as simple as QGD) that also skips communication rounds. Different from the downlink server-to-worker communications that can be performed simultaneously (e.g., by broadcasting \( \theta^k \)), the server in the uplink receives the workers’ gradients in the presence of interference, whose mitigation costs resources, e.g., extra latency or bandwidth. For this reason, our focus here is on reducing the number of worker-to-server uplink communications, which will also refer to as uploads. Our Lazily Aggregated Quantized (LAQ) GD update is given by (cf. [3])

\[
\text{LAQ:} \quad \theta^{k+1} = \theta^k - \alpha \nabla k \quad \text{with} \quad \nabla k = \nabla k - 1 + \sum_{m \in M} \delta Q_{m}^k \tag{4}
\]

where \( k \) is an approximate aggregated gradient that summarizes the parameter change at iteration \( k \), and \( \delta Q_{m}^k := Q_{m}(\theta^k) - Q_{m}(\theta^{k-1}) \) is the difference between two quantized gradients of \( f_m \) at the current iterate \( \theta^k \) and the previous copy \( \theta^{k-1} \). With a judiciously selected criterion that will be elaborated later, \( M^k \) denotes the subset of workers whose local \( \delta Q_{m}^k \) is uploaded in iteration \( k \), while the parameter vector iterates are given by \( \theta_{m}^k := \theta^k \), \( \forall m \in M^k \), and \( \theta_{m}^k := \theta^{k-1}, \forall m \notin M^k \). For worker \( m \), the copy \( \theta^{k-1} \) is employed to remember the model parameter when last time it is selected to communicate with the server.

In comparison to QGD as [3] where ‘fresh’ quantized gradient is required from each and every worker, the key idea of LAQ is to obtain \( \nabla k \) by refining the previous aggregated gradient \( \nabla k - 1 \) with the selected gradient differences \( \{\delta Q_{m}^k\}_{m \in M^k} \); that is, using only the new gradients from the selected workers in \( M^k \), while reusing the outdated
gradients from the rest of the workers. With \( \nabla^{k-1} \) stored in the server, this simple modification scales down the per-iteration communication rounds from QGD’s \( M \) to LAQ’s \( |M^k| \). Note that one round of communication through out this paper means one worker’s upload.

Compared with alternative quantization schemes, we have that i) LAQ quantizes the gradient innovation — the difference of the current gradient relative to the previous quantized gradient; and ii) LAQ skips the gradient communication — if the gradient innovation of a worker is not significant enough, the communication of this worker is skipped. We will rigorously establish that LAQ achieves the same linear convergence as GD under the strongly convex assumption on the loss function. Numerical tests will demonstrate that our approach outperforms competing methods in terms of both communication bits and rounds.

**Notation.** Bold lowercase fonts will be used to denote column vectors; \( |x|_2 \) and \( |x|_\infty \) the \( \ell_2 \)-norm and \( \ell_\infty \)-norm of \( x \), respectively; and \( |x|_i \) the \( i \)-th entry of \( x \); while \( [a] \) will stand for the floor of \( a \); and \( \lfloor \cdot \rfloor \) for the cardinality of a set or vector.

### 2 LAQ: A Lazily Aggregated Quantized Gradient Approach

With the goal of reducing the communication overhead, two complementary techniques are incorporated in our algorithm design: i) gradient innovation-based quantization; and ii) gradient innovation-based uploading or aggregation — giving the name Lazily Aggregated Quantized (LAQ) gradient. The former reduces the number of bits per upload, while the latter cuts down the number of uploads, and jointly they effect parsimony in communications. The remainder of this section elaborates further on LAQ.

#### 2.1 Gradient Innovation-based Quantization

Quantization limits the number of bits to encode a vector during communication. Suppose we use \( b \) bits to quantize each coordinate of the gradient in contrast to 32 or 64 bits used by most computers. With \( Q \) denoting the quantization operator, the quantized gradient per worker \( m \) at iteration \( k \) is \( Q_m(\theta^k) = Q(\nabla f_m(\theta^k), Q_m(\theta^{k-1})) \), which depends on the gradient \( \nabla f_m(\theta^k) \) and its previous quantization \( Q_m(\theta^{k-1}) \). The gradient is element-wise quantized by projecting to the closest point in a uniformly discretized grid. The grid is a \( p \)-dimensional hypercube with center at \( Q_m(\theta^{k-1}) \) and radius \( R^k_m = D \frac{|Q_m(\theta^{k-1})|}{|Q_m(\theta^{k-1})|_\infty} \). With \( \tau = 1/(2^b - 1) \) defining the quantization granularity, the gradient innovation \( [\nabla f_m(\theta^k)]_i - [Q_m(\theta^{k-1})]_i \), at worker \( m \) is mapped to an integer as

\[
[q_m(\theta^k)]_i = \left[ \frac{[\nabla f_m(\theta^k)]_i - [Q_m(\theta^{k-1})]_i + R^k_m}{2\tau R^k_m} \right] + \frac{1}{2}
\]

which falls in \( \{0, 1, \ldots, 2^b - 1\} \), and thus can be encoded by \( b \) bits. Note that adding \( R^k_m \) in the numerator ensures the non-negativity of \( [q_m(\theta^k)]_i \), and adding \( 1/2 \) in \( [\cdot] \) guarantees rounding to the closest point. Hence, the quantized gradient innovation at worker \( m \) is (with \( z(1) = [1 \cdots 1]^T \))

\[
\delta Q_m^k = Q_m(\theta^k) - Q_m(\theta^{k-1}) = 2R^k_m q_m(\theta^k) - R^k_m z(1)
\]

which can be transmitted by \( 32 + b \)p bits (32 bits for \( R^k_m \) and \( b \)p bits for \( q_m(\theta^k) \)) instead of the original 32p bits. With the
Algorithm 2 LAQ

1: Input: stepsize \( \alpha > 0 \), bitwidths \( \{b_m\}_{m=1}^{D} \) and \( f \).
2: Initialize: \( \theta^0 \) and \( (Q_m(\theta^0_m), t_m)_{m \in M} \).
3: for \( k = 1, 2, \ldots, K \) do
4: Server broadcasts \( \theta^k \) to all workers.
5: for \( m = 1, 2, \ldots, M \) do
6: Worker \( m \) computes \( \nabla f_m(\theta^k) \) and \( Q_m(\theta^k) \).
7: if \( \{\xi_k\}_{D=1}^{D} \) holds for worker \( m \) then
8: Worker \( m \) uploads nothing.
9: Set \( \theta^k_m = \theta^k_m - 1 \) and \( t_m \leftarrow t_m + 1 \).
10: else
11: Worker \( m \) uploads \( \delta Q_m^k \) via (6).
12: Set \( \theta^k_m = \theta^k_m \).
13: end if
14: end for
15: Server updates \( \theta \) according to (4).
16: end for

3.1 Development of the communication skipping rule

To illuminate the difference between LAQ and GD, consider re-writing (4) as

\[
\theta^{k+1} = \theta^k - \alpha [\nabla Q(\theta^k) + \sum_{m \in M^k} (Q_m(\hat{\theta}^k_m) - Q_m(\theta^k))]
\]

\[
= \theta^k - \alpha [\nabla f(\theta^k) - \epsilon^k + \sum_{m \in M^k} (Q_m(\hat{\theta}^k_m) - Q_m(\theta^k))]
\]

where \( M^k := M \setminus M^k \) denotes the subset of workers that skip communication with the server at iteration \( k \). Compared with the GD iteration in (2), the gradient employed here degrades due to the quantization error \( \epsilon^k \) and the missed gradient innovation \( \sum_{m \in M^k} (Q_m(\hat{\theta}^k_m) - Q_m(\theta^k)) \). It is clear that if a sufficiently large number of bits is used to quantize the gradient, and all \( \{\xi_k\}_{D=1}^{D} \) are set to 0, causing \( M^k = M \), then LAQ reduces to GD. Thus, adjusting \( b \) and \( \{\xi_k\}_{D=1}^{D} \) directly influences the performance of LAQ.

To compare the descent amount of LAQ with that of GD, we first establish the one step descent for both algorithms. Based on Assumption 1 the next lemma holds for GD.

Lemma 1. The GD update yields the following descent

\[
f(\theta^{k+1}) - f(\theta^k) \leq \Delta_{GD}^k
\]

where \( \Delta_{GD}^k := -(1 - \alpha L)\|\nabla f(\theta^k)\|^2_2 \).

The descent of LAQ differs from that of GD due to the quantization and selection, as specified in the next lemma. (For readability, some proofs are deferred to Section 6)

Lemma 2. The LAQ update yields the following descent

\[
f(\theta^{k+1}) - f(\theta^k) \leq \Delta_{LAQ}^k + \alpha \|\epsilon^k\|^2_2
\]

where \( \Delta_{LAQ}^k := -\frac{\alpha}{2} \|\nabla f(\theta^k)\|^2_2 + \alpha \|\sum_{m \in M^k}(Q_m(\hat{\theta}^k_m) - Q_m(\theta^k))\|^2_2 + \frac{(\frac{\alpha}{2} - \alpha)}{\|\theta^{k+1} - \theta^k\|^2_2} \|\theta^{k+1} - \theta^k\|^2_2.

At this point, it is instructive to shed more light on LAQ’s gradient skipping rule. If we fix for simplicity \( \alpha = 1/L \), it follows readily that

\[
\Delta_{LD}^k = -\frac{\alpha}{2} \|\nabla f(\theta^k)\|^2_2,
\]

\[
\Delta_{LAQ}^k = -\frac{\alpha}{2} \|\nabla f(\theta^k)\|^2_2 + \alpha \|\sum_{m \in M^k}(Q_m(\hat{\theta}^k_m) - Q_m(\theta^k))\|^2_2.
\]
The lazy aggregation criterion selects the quantized gradient improvement by assessing its contribution to the loss function decrease. For LAQ to be more communication efficient than GD, each LAQ upload should bring more descent, that is
\[
\frac{\Delta_{k,LAQ}}{|M|^k} \leq \frac{\Delta_{k,GD}}{M}. \quad (13)
\]
After simple manipulation, it can be shown that (13) boils down to
\[
\| \sum_{m \in M_k} (Q_m(\hat{\theta}^{k-1}) - Q_m(\theta^k)) \|^2 \leq \frac{|M|^k}{2M} \| \nabla f(\theta^k) \|^2 \quad (14)
\]
which implies that since
\[
\| \sum_{m \in M_k} (Q_m(\hat{\theta}^{k-1}) - Q_m(\theta^k)) \|^2 
\leq |M|^k \sum_{m \in M_k} \| (Q_m(\hat{\theta}^{k-1}) - Q_m(\theta^k)) \|^2,
\]
the following condition is sufficient to guarantee (14):
\[
\| (Q_m(\hat{\theta}^{k-1}) - Q_m(\theta^k)) \|^2 \leq \| \nabla f(\theta^k) \|^2 / (2M^2), \quad \forall m \in M_k. \quad (15)
\]
However, it is impossible to check (15) locally per worker, because the fully aggregated gradient \( \nabla f(\theta^k) \) is required, which is exactly what we want to avoid. This motivates circumventing \( \| \nabla f(\theta^k) \|^2 \) by using its approximation
\[
\| \nabla f(\theta^k) \|^2 \approx \frac{2}{\alpha} \sum_{k=1}^D \xi_k \| \theta^{k+1-d} - \theta^{k-d} \|^2
\]
which holds is that \( \nabla f(\theta^k) \) can be approximated by weighting past gradients or parameter differences since \( f(\cdot) \) is \( L \)-smooth. Combining (17) and (16) leads to (9a) with the quantization error ignored.

3.2 Convergence analysis

The rationale of the previous subsection regarding LAQ’s skipping rule is not mathematically rigorous, but we will establish here that it guarantees convergent iterates. To this end, and with \( \theta^* \) denoting the optimal solution of (1), consider the Lyapunov function associated with LAQ as
\[
\mathcal{V}(\theta^k) := f(\theta^k) - f(\theta^*) + \sum_{d=1}^D \sum_{j=d}^D \xi_j \| \theta^{k+1-d} - \theta^{k-d} \|^2 + \gamma \sum_{m \in M} \| \theta^k \|^2 \infty.
\]
Before we quantify the process of \( \mathcal{V}(\theta^k) \) in the ensuing lemma, it is worth pointing out that the Lyapunov function associated with LAQ is a strict generalization of that used in GD or LAG \([10,31]\), which not only takes into account the delayed iterates but also the quantization error.

Lemma 3. Under Assumption 1 and 2 and by fixing parameters
\[
\xi_1 = \xi_2 = \cdots = \xi, \quad \beta_d = \left( \frac{L}{L^*+1} \right), \quad \alpha = \frac{a}{L}, \quad \text{and} \quad \gamma^2 = \frac{bL}{L^*},
\]
with \( a, b > 0 \), the Lyapunov function obeys the inequality
\[
\mathcal{V}(\theta^{k+1}) \leq \sigma_1 \mathcal{V}(\theta^k) + BM \sum_{d=1}^D \xi_d \| \theta^{k+1-d} - \theta^{k-d} \|^2 + \gamma \sum_{m \in M} \| \theta^k \|^2 \infty. \quad (19)
\]
where the constant is defined as
\[
B = \left[ \frac{3a}{2L} + \frac{9a}{L} + 3D \xi + 9ab \right] \left( \frac{3a}{2L} + \frac{9a}{L} + 3D \xi + 9ab \right),
\]
and \( \sigma_1 = 1 - c \) with
\[
c = \min \left\{ \frac{1}{2} - (a + 2D \xi + 6ab) \frac{a}{L} + \frac{a}{L} \right\}.
\]

Proof. It follows from (8) that
\[
\left\| \epsilon_{m+1} \right\|^2 \leq \tau^2 \left\| \epsilon_m \right\|^2, \quad \left\| \epsilon_m \right\|^2 \leq \frac{\tau^2}{\gamma^2} \left\| \epsilon_{m-1} \right\|^2
\]
which is exactly what we want to avoid. This motivates that
\[
\left\| \nabla f(\theta^k) \right\|^2 \leq \frac{2}{\alpha} \sum_{k=1}^D \xi_k \| \theta^{k+1-d} - \theta^{k-d} \|^2
\]
where \( \{ \xi_d \}_{d=1}^D \) are constants. The main reason why (17) holds is that \( \nabla f(\theta^k) \) can be approximated by weighting past gradients or parameter differences since \( f(\cdot) \) is \( L \)-smooth. Combining (17) and (16) leads to (9a) with the quantization error ignored.
Thus, the one-step Lyapunov difference satisfies

\[
\mathbb{V}(\theta^{k+1}) - \mathbb{V}(\theta^k) \leq \frac{1}{2} \beta_1 \alpha + (L + 2\beta_1 + 6\gamma^2 L_m^2)(1 + \rho_2) \alpha^2 \|
abla f(\theta^k)\|_2^2 + \frac{1}{2\rho_1} \|e_k\|_2^2
\]

we can rewrite (23) as

\[
\mathbb{V}(\theta^{k+1}) - \mathbb{V}(\theta^k) \leq \left( \frac{\alpha}{2} + \frac{L}{2} + \beta_1 + 3\gamma^2 L_m^2 \right) \alpha^2 \|
abla f(\theta^k)\|_2^2 + \frac{3\alpha}{2} \|e_k\|_2^2 + \frac{3\alpha}{2} \|
abla f(\theta^k)\|_2^2 + \frac{1}{2\rho_1} \|e_k\|_2^2
\]

Since for any \( \rho_1 > 0 \), it holds that

\[
\mathbb{V}(\theta^{k+1}) - \mathbb{V}(\theta^k) \leq \frac{1}{2} \beta_1 \alpha + (L + 2\beta_1 + 6\gamma^2 L_m^2)(1 + \rho_2) \alpha^2 \|
abla f(\theta^k)\|_2^2 + \frac{1}{2\rho_1} \|e_k\|_2^2
\]

(25)
Following [33, Lemma 3.2], given that the Lyapunov function obeys [19] and if the following condition is satisfied
\[ \sigma_1 + B M p^2 \frac{1}{\gamma} < 1 \] (34)
then it guarantees [31] holds with \( \sigma_2 = (\sigma_1 + B M p^2 \frac{1}{\gamma})^{\frac{1}{\tau}} \).

In the sequel, we will show that we can indeed find a set of parameters that make (34) hold. For the design parameter \( D \), we impose \( D \leq \kappa \). From (20), it is obvious that the following condition
\[ \frac{1}{2} - 4(a + 2D\xi + 6ab)a \leq \frac{1}{2} - \left( \frac{1}{2} a + D\xi + 3ab \right) + \frac{3bL^2}{aL^2M} \] (35)
guarantees
\[ c = \frac{1}{2} - 4(a + 2D\xi + 6ab)a \kappa . \] (36)

Thus, we obtain \( \sigma_1 = 1 - c = 1 - \frac{1}{2} - 4(a + 2D\xi + 6ab)a \kappa \).

It can be verified that choosing \( a = \frac{1}{2} \), \( b = \frac{1}{2} \), \( D\xi = \frac{1}{50} \) and \( \tau^2 \leq \frac{b}{100M} / [M^2 M^2] + \frac{b}{50} \) is a sufficient condition for (26), (35) and (34) being satisfied. With above selected parameters, we can obtain \( \sigma_1 = 1 - \frac{1}{1000} \) and
\[ \sigma_2 = (1 - \frac{1}{1000}) + M^2 p^2 \left( \frac{93L^2}{100L^2M} + \frac{9}{10L^2} \right) \tau^2 \in (0, 1) \] (37)
which together with (51) indicates the linear convergence of the Lyapunov function and completes the proof. \( \square \)

From (37), it is obvious that if the quantization is accurate enough, i.e., \( \tau^2 \to 0 \), and no communication is skipped, i.e., \( \bar{t} = 1 \), the dependence of convergence rate on condition number is of order \( \frac{1}{\bar{t}} \), the same as the gradient descent.

Compared to the LAG analysis in [20], the analysis for LAQ is more involved, because it needs to deal with not only outdated but also quantized (inexact) gradients. The latter challenges the monotonicity of the Lyapunov function in [19], which is the building block of the analysis in [20]. We tackle this issue by i) considering the outdated gradient in the quantization; and ii) accounting for the quantization error in the new selection criterion (9). As a result, Theorem 1 establishes that LAQ retains the linear convergence rate even when quantization error is present. This is because a controlled quantization error also converges at a linear rate. As for the improvement relative to the criterion version, the convergence rate \( \sigma_2 \) is explicitly characterized by the quantization parameter \( \tau \) and the maximum communication skipping interval \( \bar{t} \).

**Proposition 1.** If under Assumption 1, we choose \( \{\xi_d\}_{d=1}^D \) to satisfy \( \xi_1 \geq \xi_2 \geq \cdots \geq \xi_D \), and define \( d_m, m \in M \) as
\[ d_m := \max_d \left\{ d | L_m^2 \leq \xi_d/(30a^2 M^2 D), d \in \{1, 2, \ldots, D\} \right\} \] (38)
it suffices for worker \( m \) to have at least \( k/(d_m + 1) \) uploads with the server until the \( k \)-th iteration.

This proposition asserts that the communication intensity per worker is determined by the smoothness of the corresponding local loss function. Workers with smaller smoothness constant communicate with the server less frequently, which justifies the term lazily communication.

For some technical issues, the current bound on the convergence rate is relatively loose in order to account for the worst-case performance. Due to the error \( e^k_m \) introduced by the communication skipping and gradient compression, it is not theoretically established that LAQ outperforms GD. However, our empirical studies will demonstrate that LAQ significantly outperforms GD in terms of communication. To prove that LAQ is more communication-efficient than GD is more challenging and is in our future agenda.

### 4 Generalizing LAQ

In this section, we broaden the scope of LAQ by developing the stochastic LAQ and the two-way communication-efficient LAQ-driven federated learning, as we elaborate next.

#### 4.1 Stochastic LAQ

Thanks to its well-documented merits in reducing complexity, stochastic gradient descent (SGD) has been widely employed by learning tasks involving large-scale training data. Here we show that LAQ can also benefit from its stochastic counterpart, namely SLAQ, that is developed with a simple modification in the criterion. Specifically, (9a) in SLAQ is replaced by
\[ ||Q_m(\theta_m^{k-1}) - Q_m(\theta^k)|| \leq \frac{1}{\alpha^2 M^2} \sum_{d=1}^D \xi_d ||\theta^{k+1-d} - \theta^{k-d}|| \]
where superscript $s$ will henceforth denote the stochastic counterpart of LAQ quantities defined so far; and $\text{var}$ is a constant. Compared with (9a), the constant added in the stochastic case is to compensate for the variance coming from the stochastic sampling. In practice, we can use the empirical variance to approximate the variance, that is, the variance computed according to the drawn samples per iteration.

Apart from the criterion, SLAQ is different from LAQ only in the local (stochastic) gradient calculation. Specifically, the worker randomly draws $S$ samples from its training set and computes the stochastic gradient as

$$
\nabla f^s_m(\theta) = \frac{1}{S} \sum_{n=1}^{S} \nabla \ell(x_{m,n}; \theta).
$$

The quantization and other operations are the same as before. The SLAQ is summarized in Algorithm 3. Following the convention, we also consider here that the global loss function is scaled by the total number of training samples.

### 4.2 Two-way quantization

So far, communication savings have been achieved by skipping uploads and quantizing the uploaded gradient innovation. A natural extension is to also quantize the model innovation in the downlink, which results in what we term Two Way Lazily Aggregated Gradient (TWO-LAQ).

Let $\delta \theta^k = Q(\theta^k, \theta^{k-1})$ describe the quantization model. First, the model innovation is quantized as $[\delta \theta^k]$, and thus we omit the details. Then, for the server to workers communication, only the quantized model innovation $\delta \theta^k$ is broadcast. With $\delta \theta^{k-1}$ stored in memory, both the server and the workers update $\theta^k$ as

$$
\bar{\theta}^k = \delta \theta^{k-1} + \delta \theta^k.
$$

Different from possible alternatives, each worker $m$ does not have the accurate model $\theta^k$. As a result, each worker has to compute the local gradient $\nabla f_m(\theta^k)$ based on $\bar{\theta}^k$. The rest follows the LAG algorithm, meaning workers quantize the gradient innovation, and upload it, if it is large enough; otherwise, they skip this upload round.

The steps of TWO-LAQ are summarized in Algorithm 4, whose implementation is illustrated in Figure 3. Comparing Figure 3 with gradient descent, TWO-LAQ improves communication efficiency at the expense of extra memory at the server and workers. Indeed, the server needs to store $\theta^k$, $\bar{\theta}^k$ and $\nabla \bar{\theta}^k$; and each worker $m$ needs to store $\delta \theta^k$, $\bar{\theta}^k$ and $Q_m(\delta \theta^k)$. In contrast, GD only requires the server to store $\theta^k$.

### 5 Numerical tests

To validate our theoretical analysis and demonstrate the performance of LAQ in improving communication efficiency for practical machine learning tasks, we evaluate our algorithm on the regularized logistic regression (LR), which is strongly convex, and a neural network (NN) classifier involving a nonconvex loss. For our experiments, we use the MNIST dataset [39], which is equally distributed across $M = 10$ workers. Throughout, we set $D = 10$, $\xi_1 = \cdots = \xi_D = 0.8/D$, and $t = 100$.

#### 5.1 Simulation setup

**LR classifier.** Consider a multi-class classifier with say $C = 10$ classes, that relies on logistic regression trained using the MNIST dataset. Each training vector $x_{m,n}$ comprises a feature-label pair $(x_{m,n}, \xi_{m,n})$, where $x_{m,n} \in \mathbb{R}^D$ is the feature vector and $x_{m,n} \in \mathbb{R}^C$ denotes the one-hot label vector. The model $\theta \in \mathbb{R}^{D \times C}$ here is a matrix, which is slightly different from previous description, and it is adopted for convenience but does not change the learning problem. The estimated probability of $(m, n)$-th sample to belong to class $i$ is given by

$$
\tilde{x}_{m,n}^i = \text{softmax}(\theta x_{m,n}^i)
$$

which can be explicitly written as

$$
[x_{m,n}^i]_i = \frac{e^{\theta x_{m,n}^i}}{\sum_{j=1}^{C} e^{\theta x_{m,n}^j}}, \quad \forall i \in \{1, 2, \cdots, C\}.
$$

The regularized logistic regression classifier relies on the following cross-entropy loss plus a regularizer

$$
\ell(x_m, \theta) = -\sum_{i=1}^{C} x_{m,n}^i \log [\tilde{x}_{m,n}^i]_i + \frac{\lambda}{2} \text{Tr}(\theta^T \theta)
$$

where $\text{Tr}(\cdot)$ denotes trace operator, and $\theta^T$ is the transpose of $\theta$. Having defined $\ell(x_m, \theta)$, the local loss functions are $f_m(\theta) = \sum_{n=1}^{N_m} \ell(x_{m,n}; \theta)$, and the global loss function is given by

$$
f(\theta) = \frac{1}{N} \sum_{m \in \mathcal{M}} f_m(\theta)
$$

where $N$ is the total number of data samples. In our tests, we set the regularizer coefficient to $\lambda = 0.01$.

**NN classifier.** In our tests, we employ a ReLU network comprising one hidden layer having 200 nodes with dimensions of the input and output layers being $784 \times 28 \times 28$ and 10, respectively. The regularizer parameter is set to $\lambda = 0.01$.

**CNN classifier.** For the test in CIFAR 10 dataset, we adopt the convolutional neural network (CNN) which consists of 3 VGG-type blocks [40]. Each block is constructed by stacking two convolutional layers with small $3 \times 3$ filters followed by a max pooling layer. The numbers of filters for the convolutional layers in the three blocks are 32, 64, and 128, respectively. ReLU activation function is used in each layer and padding is utilized on the convolutional layers to ensure the height and width of the output feature matches the inputs. Additionally, each block is followed by a dropout layer with the rate of 20%. This is followed by a fully connected layer with 128 nodes and then the softmax layer. We add an $l_2$ regularization with coefficient 0.001.
5.2 Numerical tests

Figure 4 illustrates the convergence with different number of quantization bits. It shows that utilizing fewer bits to quantize the gradient moderately increases the number of iterations, but markedly reduces the overall number of transmitted bits. To benchmark LAQ, we compare it with two classes of algorithms, namely GD and minibatch SGD ones, corresponding to the following two tests.

Parameters. For GD algorithms, we fix \( D = 10, \xi_1 = \xi_2 = \cdots = \xi_D = 0.8/D, \bar{t} = 100 \), and we set \( \alpha = 0.02 \), and \( b = 4 \) or \( 8 \) for LR and NN classifiers, respectively. For minibatch SGD algorithms, the minibath size is 500 and \( \alpha = 0.008; b = 3 \) for LR and \( b = 8 \) for NN.

Gradient-based tests. The benchmark algorithms include GD, QGD [11] and lazily aggregated gradient (LAG) [30]. Figure 5 shows the convergence of loss residual for the LR problem. Clearly, Figure 5(a) corroborates Theorem 1 namely the linear convergence for the strongly convex loss function. As illustrated in Figure 5(b), LAQ incurs a smaller number of communication rounds than GD and QGD thanks to our innovation selection rule, yet more rounds than LAG due to the quantization error. Nevertheless, the total number of transmitted bits of LAQ is significantly reduced compared with that of LAG, as demonstrated in Figure 5(c). For the NN classifier, Figure 6 reports the convergence of the gradient norm, where LAQ also shows competitive performance for nonconvex loss functions. Similar to what is observed for LR classification, LAQ outperforms the benchmark algorithms in terms of transmitted bits. TWO-LAQ which additionally leverages model innovation quantization saves more bits than LAQ as show in Figures 5(c) and 5(c). Table 1 summarizes the detailed comparison of mentioned algorithms.
including the number of iterations, uploads and bits needed to reach a given accuracy.

**Tests on more datasets.** Figure 7 exhibits the test accuracy of the aforementioned algorithms on three commonly used datasets, namely MNIST, ijcnn1 and covtype. Applied to all these datasets, LAQ saves transmitted bits while maintaining the same accuracy. In addition, we test our algorithm on more challenging dataset—CIFAR 10, for which CNN is utilized and Adam [11] is applied. The convergence of the loss function is plotted in Figure 8 and the validation accuracy is shown in Figure 11. A detailed comparison with above mentioned benchmark algorithms is summarized in Table 2. These tests with different datasets and different algorithms (gradient descent, Adam and the following stochastic gradient descent) all demonstrate that the proposed communication saving scheme indeed provides satisfied improvement in communication efficiency and thus has promising potential for variety of distributed learning applications.

**Stochastic gradient-based tests.** The stochastic version of LAQ abbreviated as SLAQ is tested and compared with stochastic gradient descent (SGD), quantized stochastic gradient descent (QSGD) [10], sparsified stochastic gradient descent (SSGD) [21], deep gradient compression (DGC) [18], sign-SGD, [8] and tern-Grad [12]. For the all the stochastic-based algorithms, each worker draws a bath of 500 data samples to calculate a stochastic local gradient per iteration. As demonstrated in Figures 9 and 10 SLAQ requires the lowest number of communication rounds and bits. Albeit sign-SGD and tern-Grad need only 1 bit and 2 bits for each entry of the gradient, respectively, they have larger quantization error and require a smaller stepsize to ensure convergence. Therefore it takes more iterations for these two algorithms to reach the same loss (or accuracy), and needs to transmit more bits than that for SLAQ. In this stochastic gradient test, although the improvement of communication efficiency by SLAQ is not as evident as LAQ compared with GD-based algorithms, SLAQ still outperforms the cutting-edge techniques for distributed learning.

**TABLE 1**
Comparison of gradient-based algorithms. For logistic regression, all algorithms terminate when loss residual reaches $10^{-6}$; for neural network, all algorithms run a fixed number of iterations.

<table>
<thead>
<tr>
<th>Algorithm</th>
<th>Iteration #</th>
<th>Communication #</th>
<th>Bit #</th>
<th>Accuracy</th>
</tr>
</thead>
<tbody>
<tr>
<td>LAQ</td>
<td>2626</td>
<td>572</td>
<td>$6.78 \times 10^8$</td>
<td>0.9082</td>
</tr>
<tr>
<td>TWO-LAQ</td>
<td>2576</td>
<td>734</td>
<td>$1.04 \times 10^8$</td>
<td>0.9082</td>
</tr>
<tr>
<td>GD</td>
<td>2763</td>
<td>27630</td>
<td>$7.63 \times 10^7$</td>
<td>0.9082</td>
</tr>
<tr>
<td>QGD</td>
<td>2760</td>
<td>27600</td>
<td>$1.56 \times 10^7$</td>
<td>0.9082</td>
</tr>
<tr>
<td>LAG</td>
<td>2620</td>
<td>2431</td>
<td>$1.27 \times 10^7$</td>
<td>0.9082</td>
</tr>
<tr>
<td>LAQ</td>
<td>8000</td>
<td>32729</td>
<td>$8.23 \times 10^6$</td>
<td>0.9433</td>
</tr>
<tr>
<td>TWO-LAQ</td>
<td>8000</td>
<td>30741</td>
<td>$4.93 \times 10^6$</td>
<td>0.9433</td>
</tr>
<tr>
<td>GD</td>
<td>8000</td>
<td>80000</td>
<td>$4.48 \times 10^5$</td>
<td>0.9433</td>
</tr>
<tr>
<td>QGD</td>
<td>8000</td>
<td>80000</td>
<td>$1.42 \times 10^5$</td>
<td>0.9433</td>
</tr>
<tr>
<td>LAG</td>
<td>8000</td>
<td>30818</td>
<td>$1.98 \times 10^4$</td>
<td>0.9433</td>
</tr>
</tbody>
</table>

**TABLE 2**
Tests for CIFAR 10 with CNN

<table>
<thead>
<tr>
<th>Algorithm</th>
<th>Iteration #</th>
<th>Communication #</th>
<th>Bit #</th>
<th>Accuracy</th>
</tr>
</thead>
<tbody>
<tr>
<td>LAQ</td>
<td>1000</td>
<td>6359</td>
<td>$3.34 \times 10^8$</td>
<td>87.96</td>
</tr>
<tr>
<td>TWO-LAQ</td>
<td>1000</td>
<td>5785</td>
<td>$2.76 \times 10^8$</td>
<td>87.92</td>
</tr>
<tr>
<td>GD</td>
<td>1000</td>
<td>10000</td>
<td>$1.09 \times 10^8$</td>
<td>87.86</td>
</tr>
<tr>
<td>QGD</td>
<td>1000</td>
<td>10000</td>
<td>$4.69 \times 10^7$</td>
<td>87.95</td>
</tr>
<tr>
<td>LAG</td>
<td>1000</td>
<td>6542</td>
<td>$7.44 \times 10^7$</td>
<td>87.91</td>
</tr>
</tbody>
</table>

Fig. 7. Tests on different datasets
Fig. 8. Convergence of loss function (CNN for CIFAR 10)

Fig. 9. Convergence of loss function (logistic regression)

Fig. 10. Convergence of loss function (neural network)

<table>
<thead>
<tr>
<th>Algorithm</th>
<th>Iteration #</th>
<th>Communication #</th>
<th>Bit #</th>
<th>Accuracy</th>
</tr>
</thead>
<tbody>
<tr>
<td>Logistic</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>SLAQ</td>
<td>1000</td>
<td>4494</td>
<td>$1.06 \times 10^8$</td>
<td>0.9060</td>
</tr>
<tr>
<td>SGD</td>
<td>1000</td>
<td>10000</td>
<td>$2.51 \times 10^7$</td>
<td>0.9044</td>
</tr>
<tr>
<td>QSGD</td>
<td>1000</td>
<td>10000</td>
<td>$6.89 \times 10^7$</td>
<td>0.9062</td>
</tr>
<tr>
<td>SSGD</td>
<td>1000</td>
<td>10000</td>
<td>$1.26 \times 10^8$</td>
<td>0.9056</td>
</tr>
<tr>
<td>DGC</td>
<td>1000</td>
<td>10000</td>
<td>$5.21 \times 10^7$</td>
<td>0.9082</td>
</tr>
<tr>
<td>sign-SGD</td>
<td>2000</td>
<td>20000</td>
<td>$1.57 \times 10^8$</td>
<td>0.8905</td>
</tr>
<tr>
<td>tern-Grad</td>
<td>2000</td>
<td>20000</td>
<td>$3.14 \times 10^8$</td>
<td>0.8942</td>
</tr>
<tr>
<td>Neural network</td>
<td>1500</td>
<td>4342</td>
<td>$4.14 \times 10^8$</td>
<td>0.9360</td>
</tr>
<tr>
<td>SLAQ</td>
<td>1500</td>
<td>15000</td>
<td>$7.63 \times 10^7$</td>
<td>0.9354</td>
</tr>
<tr>
<td>SGD</td>
<td>1500</td>
<td>15000</td>
<td>$3.84 \times 10^7$</td>
<td>0.9353</td>
</tr>
<tr>
<td>QSGD</td>
<td>1500</td>
<td>15000</td>
<td>$1.14 \times 10^8$</td>
<td>0.9356</td>
</tr>
<tr>
<td>SSGD</td>
<td>1500</td>
<td>15000</td>
<td>$3.60 \times 10^7$</td>
<td>0.9362</td>
</tr>
<tr>
<td>DGC</td>
<td>1500</td>
<td>15000</td>
<td>$4.77 \times 10^8$</td>
<td>0.9277</td>
</tr>
<tr>
<td>sign-SGD</td>
<td>3000</td>
<td>30000</td>
<td>$9.54 \times 10^8$</td>
<td>0.9299</td>
</tr>
<tr>
<td>tern-Grad</td>
<td>3000</td>
<td>30000</td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

TABLE 3

Performance comparison of mini-batch stochastic gradient-based algorithms.
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This paper investigated communication-efficient federated learning, and developed LAQ — an approach that integrates quantization and adaptive communication techniques based on gradient innovation. Compared with GD method, LAQ introduces errors to gradient, yet still preserves linear convergence for strongly convex problems. This is a remarkable result considering that LAQ significantly reduces both communication bits and rounds. Experiments on strongly convex and nonconvex learning problems verified our theoretical analysis and demonstrated the merits of LAQ over recent popular approaches. Furthermore, two variants of LAQ, termed TWO-LAQ and SLAQ, also exhibit promising performance and outperform prevalent compression schemes in the empirical studies.

6 CONCLUSIONS

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7 ACKNOWLEDGEMENTS

8 PROOFS

8.1 Proof of Lemma 2

For successive LAQ updates, it is not difficult to show that

\[
\begin{align*}
& f(\theta^{k+1}) - f(\theta^k) \\
\leq & \left\langle \nabla f(\theta^k), -\alpha \left[ \nabla f(\theta^k) - \varepsilon^k + \sum_{m \in M_k^c} (Q_m(\theta^{k-1}_m) - Q_m(\theta^k)) \right] \right\rangle \\
& + \frac{L}{2} \| \theta^{k+1} - \theta^k \|^2 \\
\leq & -\alpha \| \nabla f(\theta^k) \|^2 + \frac{L}{2} \| \theta^{k+1} - \theta^k \|^2 \\
& + \alpha \left\langle \nabla f(\theta^k), \varepsilon^k - \sum_{m \in M_k^c} (Q_m(\theta^{k-1}_m) - Q_m(\theta^k)) \right\rangle \\
= & -\alpha \| \nabla f(\theta^k) \|^2 - \frac{1}{2\alpha} \| \theta^{k+1} - \theta^k \|^2 + \frac{L}{2} \| \theta^{k+1} - \theta^k \|^2 \\
& + \alpha \left\langle \nabla f(\theta^k), \varepsilon^k - \sum_{m \in M_k^c} (Q_m(\theta^{k-1}_m) - Q_m(\theta^k)) \right\rangle \\
\leq & -\alpha \| \nabla f(\theta^k) \|^2 + \frac{1}{2\alpha} \left\| Q_m(\theta^{k-1}_m) - Q_m(\theta^k) \right\|_2^2
\end{align*}
\]

where the second equality follows from the identity \( \langle a, b \rangle = \frac{1}{2} (\| a \|^2 + \| b \|^2 - \| a - b \|^2) \), and the last inequality inequality from the fact that \( \sum_{i=1}^n \alpha_i \| \xi_i \|^2 \leq n \sum_{i=1}^n \| \xi_i \|^2 \).

8.2 Proof of Proposition 1

Suppose that at current iteration \( k \) the last iteration when worker \( m \) communicated with the server is \( d' \), where \( 1 \leq d' \leq d_m \). Having \( \theta^{k-1}_m = \theta^{k-d'} \), we thus deduce that

\[
\begin{align*}
& \| Q_m(\theta^{k-1}_m) - Q_m(\theta^k) \|_2^2 \\
= & \| Q_m(\theta^{k-d'} - d') - Q_m(\theta^k) \|_2^2 + \| \nabla f_m(\theta^k) \|_2^2 \\
& + \| \nabla f_m(\theta^{k-d'}) - \nabla f_m(\theta^k) \|_2^2 \\
\leq & 3 \left\| f_m(\theta^{k-d'}) - f_m(\theta^k) \right\|_2^2 + \| \varepsilon^k \|_2^2 + \| \varepsilon^{k-d'} \|_2^2 \\
\leq & 3 \left( L_m^d \| \theta^{k-d'} - \theta^k \|_2^2 + \| \varepsilon^k \|_2^2 + \| \varepsilon^{k-d'} \|_2^2 \right) \\
= & 3 \left( L_m^d \| \hat{\theta}^{k-d'} - \hat{\theta}^k \|_2^2 + \| \varepsilon^k \|_2^2 + \| \varepsilon^{k-d'} \|_2^2 \right)
\end{align*}
\]

From the definition of \( d_m \) and since \( \xi_1 \geq \xi_2 \geq \cdots \geq \xi_D \), it can be inferred that

\[
L_m^d \leq \frac{\xi_d}{3\alpha^2 M^2 D}, \quad \text{for all } d' \text{ satisfying } 1 \leq d' \leq d_m.
\]

Substituting (47) into (46) yields

\[
\begin{align*}
& \| Q_m(\theta^{k-1}_m) - Q_m(\theta^k) \|_2^2 \\
\leq & \frac{\xi_d}{\alpha^2 M^2} \sum_{d=1}^{d_m} \xi_d \| \hat{\theta}^{k-d'} - \hat{\theta}^k \|_2^2 + 3 \left( \| \varepsilon^k \|_2^2 + \| \varepsilon^{k-d'} \|_2^2 \right) \\
\leq & \frac{1}{\alpha^2 M^2} \sum_{d=1}^{d_m} \xi_d \| \hat{\theta}^{k-d'} - \hat{\theta}^k \|_2^2 + 3 \left( \| \varepsilon^k \|_2^2 + \| \varepsilon^{k-d'} \|_2^2 \right)
\end{align*}
\]

which exactly implies that (9a) is satisfied. Since \( d_m \leq D \leq t \), the criterion (7) holds, which means that worker \( m \) will not upload her/his information until at least \( t \) iterations after...
last upload. In the first $k$ iterations, worker $m$ will therefore have at most $k/(d_m + 1)$ uploads to the server.

**REFERENCES**


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